

Transcomputation - Exercise 5

Dr James A.D.W. Anderson FBCS CITP CSci

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Note

Polar-transcomplex multiplication and division are lexically identical to their polar-complex counterparts:

$$\begin{aligned}(r_1, \theta_1) \times (r_2, \theta_2) &= (r_1 r_2, \theta_1 + \theta_2) \\ (r_1, \theta_1) \div (r_2, \theta_2) &= (r_1 / r_2, \theta_1 - \theta_2)\end{aligned}$$

Rotation of a polar point (r, ϕ) by θ radians is identical to multiplication of the polar point by $(1, \theta)$.

1 Calculate Rotations

- 1.1 Rotate the polar point $(1, 0)$ by 0 radians.
- 1.2 Rotate the polar point $(1, 0)$ by $\pi/2$ radians.
- 1.3 Rotate the polar point $(1, \pi/2)$ by $-\pi/2$ radians.
- 1.4 Rotate the polar point $(1, 2)$ by ∞ radians.
- 1.5 Calculate the polar points corresponding to a square with Cartesian co-ordinates $(0, 0)$, $(1, 0)$, $(1, 1)$, $(0, 1)$.
- 1.6 Rotate the square in part (1.5) immediately above by $\pi/4$ radians.

2 Sketching

Sketch points and figures on a Cartesian plane of (x, y) co-ordinates.

- 2.1 Sketch the rotation of the point in part (1.1) above.
- 2.2 Sketch the rotation of the point in part (1.2) above.
- 2.3 Sketch the rotation of the point in part (1.3) above.
- 2.4 Sketch the rotation of the point in part (1.4) above.
- 2.5 Sketch the rotation of the square in part (1.6) above.